

HW 27

pl17

f.

$$\begin{aligned}
 43. \quad & 9x^2 - 18x + 3 = 0 \\
 & 9(x^2 - 2x + 1) - 9 + 3 = 0 \\
 & 9(x-1)^2 - 6 = 0 \\
 & (x-1)^2 = \frac{6}{9} \\
 & (x-1)^2 = \frac{2}{3} \\
 & x-1 = \pm \sqrt{\frac{2}{3}}
 \end{aligned}$$

$$x = \pm \sqrt{\frac{2}{3}} + 1$$

$$\begin{aligned}
 44. \quad & 4x^2 - 4x - 1 = 0 \\
 & 4(x^2 - x + \frac{1}{4}) - 1 - 1 = 0 \\
 & 4(x - \frac{1}{2})^2 - 2 = 0 \\
 & (x - \frac{1}{2})^2 = \frac{2}{4} \\
 & x - \frac{1}{2} = \pm \sqrt{\frac{2}{4}}
 \end{aligned}$$

$$x = \frac{1 \pm \sqrt{2}}{2}$$

$$\begin{aligned}
 45. \quad & -x^2 + 2x + 7 = 0 \\
 & -1(x^2 - 2x + 1) + 1 + 8 = 0 \\
 & -1(x-1)^2 + 9 = 0 \\
 & -1(x-1)^2 = -9 \\
 & (x-1)^2 = 9 \\
 & x-1 = \pm 3 \\
 & x = 1 \pm 3 \\
 & \boxed{x = 4} \\
 & \boxed{x = -2}
 \end{aligned}$$

$$\begin{aligned}
 45. \quad & D = (-5)^2 - 4(2)(5) \\
 & D = 25 - 40 \\
 & D = -15 \\
 & \text{no real roots}
 \end{aligned}$$

$$\begin{aligned}
 46. \quad & D = (-4)^2 - 4(-5)(1) \\
 & D = 16 + 20 \\
 & D = 36 \\
 & \text{2 real roots}
 \end{aligned}$$

$$\begin{aligned}
 47. \quad & D = (-1)^2 - 4(2)(1) \\
 & D = 1 + 8 = 9 \\
 & \text{2 real roots}
 \end{aligned}$$

$$\begin{aligned}
 48. \quad & D = (-4)^2 - 4(1)(4) \\
 & D = 16 - 16 \\
 & D = 0 \\
 & \text{1 real root}
 \end{aligned}$$

$$49. \quad x = \frac{-12 \pm \sqrt{12^2 - 4(1)(16)}}{2(1)}$$

$$x = \frac{-12 \pm \sqrt{80}}{2}$$

$$x = \frac{-12 \pm 4\sqrt{5}}{2}$$

$$\boxed{x = -6 \pm 2\sqrt{5}}$$

$$80. x^2 + 4x - 8 = 0$$

$$x = \frac{-4 \pm \sqrt{16 - 4(1)(-8)}}{2(1)}$$

$$x = \frac{-4 \pm \sqrt{48}}{2}$$

$$x = \frac{-4 \pm 4\sqrt{3}}{2}$$

$$x = -2 \pm 2\sqrt{3}$$

$$83. 0 = 9x^2 - 12x - 3$$

$$x = \frac{12 \pm \sqrt{144 - 4(9)(-3)}}{2(9)}$$

$$x = \frac{12 \pm \sqrt{252}}{18}$$

$$x = \frac{12 \pm 6\sqrt{7}}{18}$$

$$x = \frac{2 \pm \sqrt{7}}{3}$$

$$81. x = \frac{-8 \pm \sqrt{64 - 4(1)(-4)}}{2}$$

$$x = \frac{-8 \pm \sqrt{80}}{2}$$

$$x = \frac{-8 \pm 4\sqrt{5}}{2}$$

$$x = -4 \pm 2\sqrt{5}$$

$$82. x = \frac{3 \pm \sqrt{9 - 4(2)(-4)}}{2}$$

$$x = \frac{3 \pm \sqrt{41}}{2(2)}$$

$$x = \frac{3 \pm \sqrt{41}}{4}$$

144. a) iv
b) ~~iii~~ iii
c) i
d) ii

$$145. y = (x-3)(x+5)$$

$$146. y = (x+6)(x+9)$$

$$147. y = (x-8)(x-14)$$

$$148. y = (6x-1)(5x+2)$$